## Harmonical

Given three diverging lines, how to find the fourth harmonical?


The lines $A B, A C$ and $A D$ diverge. If $E$ is on $B C$ and $A D$, and $F$ is on $A B$ and $C D$, and $G$ is on $E F$ and $B D$, then $A G$ is the fourth harmonical.

The point $G$ does not depend on the choice of $C$, and the line $A G$ does not depend on the choice of $B, D$ (as long as $B, C, D$ are on the given lines, and are not equal to $A$ ).

Note that the points on any line which intersects the four lines through A are harmonic conjugates. For exampe, if $H$ is the intersection of $B D$ and $A C$, then $H, G$ are harmonic conjugates with respect to $B, D$.

